

Calcolo del dominio di una funzione

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Gli esercizi sono proposti in ordine di difficoltà crescente.

nota: in un file così lungo e complesso può accadere che sia presente un errore di diversa natura nonostante gli esercizi siano stati controllati più volte. Saremo grati di ricevere segnalazioni di eventuali refusi o suggerimenti di qualsiasi natura.

Nelle soluzioni degli esercizi goniometrici la lettera **k** rappresenta un numero intero cioè $k \in \mathbb{Z}$ tranne ove diversamente specificato

funzioni algebriche



1	$y = x^3 - 2x^2 - 3x$	\mathbb{R}
2	$y = \frac{3x + 1}{2}$	\mathbb{R}
3	$y = \frac{8x - 5}{x}$	$x \neq 0$
4	$y = \frac{5}{2x + 3}$	$x \neq -\frac{3}{2}$
5	$y = \frac{2 - 4x + x^3}{5 - x}$	$x \neq 5$
6	$y = 2x^8 + 52x^2 + 6$	\mathbb{R}
7	$y = \frac{3x^5 - 4x^4 + 3x^2 - 6}{x^2 + 5}$	\mathbb{R}
8	$y = \frac{3x^2 + 2}{2x - 3}$	$x \neq \frac{3}{2}$
9	$y = \frac{x^2 + 5}{x^3}$	$x \neq 0$
10	$y = 3x^3 - 5x^2 + 1$	\mathbb{R}

11	$y = \frac{3}{x-1}$	$x \neq 1$
12	$y = \frac{1}{x^2}$	$x \neq 0$
13	$y = \frac{3x+1}{2x-1}$	$x \neq \frac{1}{2}$
14	$y = \frac{x^2+x-1}{x+2}$	$x \neq -2$
15	$y = x^3 - \frac{x}{2} + 1$	R
16	$y = \sqrt{x+3}$	$x \geq -3$
17	$y = \sqrt{x-1}$	$x \geq 1$
18	$y = \sqrt[3]{x^2-2x+6}$	R
19	$y = \sqrt{x-3}$	$x \geq 3$
20	$y = \sqrt[3]{4-2x}$	R

21	$y = \frac{4 - 8x}{\sqrt{6 + x^2}}$	\mathbb{R}
22	$y = \frac{x^2 - \sqrt{2}}{x^2 - 4}$	$x \neq \pm 2$
23	$y = \frac{\sqrt{x} - 3}{x - 2}$	$0 \leq x < 2 \vee x > 2$
24	$y = \frac{2x - 1}{7 - x^2}$	$x \neq -\sqrt{7} \wedge x \neq +\sqrt{7}$
25	$y = x^3 - 2x^2 - 3x - 2$	\mathbb{R}
26	$y = \frac{1 - x^2}{x^2 + x + 3}$	\mathbb{R}
27	$y = \sqrt{x^2 - 2x - 2}$	$x \leq 1 - \sqrt{3} \vee x \geq 1 + \sqrt{3}$
28	$y = \sqrt[5]{\frac{x^2 - 1}{x^2 - 4x + 3}}$	$x \neq 1 \wedge x \neq 3$
29	$y = \frac{x^2 + 5}{x^2 + x - 6}$	$x \neq -3 \wedge x \neq 2$
30	$y = \frac{x + 9}{x^2 + 2x + 1}$	$x \neq -1$

31	$y = \frac{\sqrt{-1+x}}{x^2+x+1}$	$x \geq 1$
32	$y = \frac{x+3}{x^2-1}$	$x \neq -1 \wedge x \neq 1$
33	$y = \frac{3x-1}{x^2-5x+6}$	$x \neq 2 \wedge x \neq 3$
34	$y = \frac{8x-1}{\sqrt{x+2}}$	$x > -2$
35	$y = \frac{\sqrt{x-1}}{x+1}$	$x \geq 1$
36	$y = \frac{x^2-5x}{\sqrt[3]{4-x}}$	$x \neq 4$
37	$y = \sqrt[3]{\frac{x+2}{x-6}}$	$x \neq 6$
38	$y = \frac{\sqrt[3]{x-1}}{2x+5}$	$x \neq -\frac{5}{2}$
39	$y = \sqrt{x-3} + \sqrt[3]{x+1}$	$x \geq 3$
40	$y = \sqrt[5]{x^3+4x^2-2} \cdot \sqrt{x}$	$x \geq 0$

41	$y = \sqrt{4 - x^2}$	$-2 \leq x \leq 2$
42	$y = \sqrt{\frac{2 + x^2}{x}}$	$x > 0$
43	$y = \sqrt{\frac{x + 1}{x - 1}}$	$x \leq -1 \vee x > 1$
44	$y = \sqrt{\frac{1 + x^2}{-3}}$	\emptyset
45	$y = \frac{x^2 - x + 1}{x^2 - 7x + 12}$	$x \neq 3 \wedge x \neq 4$
46	$y = \sqrt{1 + x^2}$	\mathbb{R}
47	$y = \frac{x - 4}{ x + 5 }$	$x \neq -5$
48	$y = \frac{x + 5}{x^4 + 2}$	\mathbb{R}
49	$y = \frac{x}{ x - 5 }$	$x \neq 5$
50	$y = \sqrt[9]{\frac{5 - x}{ x - 1 }}$	$x \neq 1$

51	$y = \frac{(x^2 - 1) \sqrt[3]{x^5 - 2}}{x \sqrt[4]{2 - x}}$	$x < 2 \wedge x \neq 0$
52	$y = \sqrt{x + 1} + \sqrt{x^2 - 5}$	$x \geq \sqrt{5}$
53	$y = \sqrt{1 - x^2}$	$-1 \leq x \leq 1$
54	$y = \frac{x\sqrt{x - 3}}{x^2 - 16}$	$3 \leq x < 4 \vee x > 4$
55	$y = \sqrt{\frac{x - 1}{x(x + 1)}}$	$-1 < x < 0 \vee x \geq 1$
56	$y = \sqrt{x^2 - 4}$	$x \leq -2 \vee x \geq 2$
57	$y = \frac{1}{\sqrt{x^2 + 1}}$	R
58	$y = \sqrt{9 - x^2} + \frac{5}{x}$	$-3 \leq x < 0 \vee 0 < x \leq 3$
59	$y = \frac{1}{\sqrt{x^2 - 3x}}$	$x < 0 \vee x > 3$
60	$y = \sqrt{ x }$	R


61	$y = \frac{x^2 - 5x + 6}{x^2 - 3x + 10}$	R
62	$y = \frac{2x^2 - x + 3}{-3x^2 + 16x - 5}$	$x \neq \frac{1}{3} \wedge x \neq 5$
63	$y = \frac{3x^2 + 5x - 2}{3x^2 - x - 14}$	$x \neq -2 \wedge x \neq \frac{7}{3}$
64	$y = \frac{x^3 - 1}{x^2 + x - 2}$	$x \neq -2 \wedge x \neq 1$
65	$y = \frac{x^2 - 3x}{x^3 - 8}$	$x \neq 2$
66	$y = \frac{\sqrt[3]{x - \frac{1}{2}}}{x}$	$x \neq 0$
67	$y = x^2 + x - 9 $	R
68	$y = \sqrt{x^2 - 6x}$	$x \leq 0 \vee x \geq 6$
69	$y = \sqrt[4]{x^2 + 5}$	R
70	$y = \sqrt[5]{\frac{x}{x^3 - 1}}$	$x \neq 1$

71	$y = \sqrt[3]{\frac{3x-6}{3- x }} + \frac{6x}{\sqrt[5]{x-2}}$	$x \neq -3 \wedge x \neq 2 \wedge x \neq 3$
72	$y = \frac{4x^2}{\sqrt{4-x}} - \frac{2x}{\sqrt{2x-3}}$	$\frac{3}{2} < x < 4$
73	$y = \frac{x+1}{\sqrt{x^2-6x+9}}$	$x \neq 3$
74	$y = \frac{5x^4-3x+3}{\sqrt[7]{2-x}} - \frac{x^2-2x+1}{\sqrt{x^2-6x+9}}$	$x \neq 2 \wedge x \neq 3$
75	$y = \frac{\sqrt[3]{2-x}}{\sqrt[4]{x^4-81}}$	$x \leq -3 \vee x \geq 3$
76	$y = \sqrt{x-3 x }$	0
77	$y = \frac{x^2-3}{e- x^2-1 }$	$x \neq \pm\sqrt{1+e}$
78	$y = \frac{3x^2-2}{ x+1 -5}$	$x \neq -6 \wedge x \neq 4$
79	$y = \frac{\sqrt{x^2+3}}{ x^2-1 +3x}$	$x \neq \frac{-3-\sqrt{13}}{2} \wedge x \neq \frac{3-\sqrt{13}}{2}$
80	$y = \sqrt{8-x^2} + \sqrt{x-1} + \sqrt{x}$	$1 \leq x \leq 2\sqrt{2}$

81	$y = \sqrt{ 5 - 2x - 4 - x}$	$x \leq \frac{1}{3} \vee x \geq 9$
82	$y = \frac{x - 7}{x^2 - 2 x - 3}$	$x \neq -3 \wedge x \neq 3$
83	$y = \sqrt{\frac{2x + 3}{x - 1}}$	$x \leq -\frac{3}{2} \vee x > 1$
84	$y = \sqrt{\sqrt{x - 1} - x + 3}$	$1 \leq x \leq 5$
85	$y = \sqrt{2x - 1 + x + 1 }$	$x \geq 0$
86	$y = \frac{3x + 1}{x^3 - x}$	$x \neq -1 \wedge x \neq 0 \wedge x \neq 1$
87	$y = \frac{1}{\sqrt{ x - 1 }}$	$x \neq 1$
88	$y = \sqrt{ x - x^2}$	$-1 \leq x \leq 1$
89	$y = \frac{2}{x - 1} - \frac{1}{x} - \frac{1}{x^2 - x}$	$x \neq 0 \wedge x \neq 1$
90	$y = \frac{3x}{2 x - 1}$	$x \neq -\frac{1}{2} \wedge x \neq \frac{1}{2}$

91	$y = \sqrt{x^2 - 1} + \sqrt{x - 5}$	$x \geq 5$
92	$y = \frac{x + \sqrt{x + 1}}{\sqrt{x - 2}}$	$x > 2$
93	$y = \frac{\sqrt{x^2 + 3} - \sqrt{x + 7}}{x^2 - 4x + 4}$	$-7 \leq x < 2 \vee x > 2$
94	$y = \frac{x - 1}{ x - 3 + x + 1 }$	R
95	$y = \frac{3 + x}{ x + 2 + x^2 - x - 6 }$	$x \neq -2$
96	$y = \frac{ x + 5 }{ x - 1 - x - 2 }$	$x \neq \frac{3}{2}$
97	$y = \frac{\sqrt[4]{x - x^2}}{\sqrt{x^2 + 3}}$	$0 \leq x \leq 1$
98	$y = \sqrt{x^3 - 3x} + \sqrt[3]{x^2 - 3x - 4}$	$-\sqrt{3} \leq x \leq 0 \vee x \geq \sqrt{3}$
99	$y = \frac{3x^2 + 5x - 2}{\sqrt{x + 5} - 4}$	$-5 \leq x < 11 \vee x > 11$
100	$y = \frac{2x + x^2}{\sqrt{x^2 - 8}} + \sqrt{6 - x^2}$	\emptyset

101	$y = \sqrt{\frac{x^3(x-1)^2}{x+3}}$	$x < -3 \vee x \geq 0$
102	$y = \sqrt[20]{1 - 4 - 3x }$	$1 \leq x \leq \frac{5}{3}$
103	$y = \frac{x^2 - 2 + 1}{6x - x^2 - 4 }$	$x \neq \pm 3 + \sqrt{13}$
104	$y = \frac{\sqrt{2+x^2}}{\sqrt[11]{-3x - \sqrt{1+x^2}}}$	$x \neq -\frac{\sqrt{2}}{4}$
105	$y = \frac{2 - \sqrt[3]{3 x - x + 1}}{\sqrt{4 - x }}$	$-4 < x < 4$
106	$y = \frac{\sqrt{1 - \frac{e^2}{x}}}{\sqrt[5]{x^2 - 9}}$	$x < 0 \vee x > e^2 \wedge x \neq -3$
107	$y = \sqrt{\frac{3x - x + 4 - 1}{6 - 1 - x^2 }}$	$x < -\sqrt{7} \vee \frac{5}{2} \leq x < \sqrt{7}$
108	$y = \frac{\sqrt{x+3}}{\sqrt{ x+1 -2}} + 1$	$x > 1$
109	$y = \frac{1}{\sqrt{ x }} + \frac{1}{ x^2 - 1 } + \sqrt{2-x}$	$x < 2 \wedge x \neq 0 \wedge x \neq \pm 1$
110	$y = \frac{\sqrt{16-x^2}}{x^2 - 6x + 9} + \frac{x}{\sqrt{x^2 - 16}}$	\emptyset

111	$y = \sqrt{1 - \sqrt{x}} + \sqrt[3]{x + 1}$	$0 \leq x \leq 1$
112	$y = \frac{\sqrt{4x - 6}}{\sqrt[3]{x^2(x - 8)}} + \sqrt[3]{\frac{1}{4 - x }}$	$x \geq \frac{3}{2} \wedge x \neq 4 \wedge x \neq 8$
113	$y = \sqrt{2x - \sqrt{3 - 4x}}$	$\frac{1}{2} < x \leq \frac{3}{4}$
114	$y = \frac{3 - x^2}{\sqrt[6]{2x - 1 - 4x }}$	$\frac{1}{6} < x < \frac{1}{2}$
115	$y = \frac{3x^3 + 1}{ 3x - 1 + 2} + \frac{2 - x }{\sqrt{4x - 1}}$	$x > \frac{1}{4}$
116	$y = \sqrt[4]{x - 2 + 23 x + 1 - 2x - 1 }$	$x \leq -\frac{13}{10} \vee x \geq -\frac{10}{13}$
117	$y = \sqrt{\frac{ -2x - 1 - 3}{x^2 + 2x - 1}}$	$x < -\sqrt{2} - 1 \vee 2 \leq x < \sqrt{2} - 1 \vee x \geq 1$
118	$y = \sqrt{\sqrt{3 - x^2} - \sqrt{2 - x}}$	$\frac{1 - \sqrt{5}}{2} \leq x \leq \frac{1 + \sqrt{5}}{2}$
funzioni logaritmiche ed esponenziali 		
119	$y = \log(x - 3)$	$x > 3$
120	$y = \log_2(5 - x) + 1$	$x < 5$

121	$y = e^{5-x}$	R
122	$y = \log \frac{x^2 + 5}{3}$	R
123	$y = 8^{\frac{5}{x-2}}$	$x \neq 2$
124	$y = \log_{\frac{1}{2}} \sqrt{x-8}$	$x > 8$
125	$y = 3^{\frac{x-1}{5-x}}$	$x \neq 5$
126	$y = \log_{\frac{2}{3}}(1-x)$	$x < 1$
127	$y = 5^{\frac{5x^2-1}{5x-1}}$	$x \neq \frac{1}{5}$
128	$y = \log_{\frac{1}{2}} \frac{x-3}{1-x}$	$1 < x < 3$
129	$y = e^{\frac{x+3}{x-1}}$	$x \neq 1$
130	$y = \sqrt{2^{2x} - 2^x}$	$x \geq 0$
131	$y = e^{\frac{x+3}{x-1}}$	$x \neq 1$
132	$y = \frac{3^{2x} + 5^{\frac{3x}{x-1}}}{x + \frac{1}{2}}$	$x \neq -\frac{1}{2} \wedge x \neq 1$


133	$y = \sqrt{\ln(x+1)}$	$x \geq 0$
134	$y = \sqrt{e^{x-1}}$	\mathbb{R}
135	$y = e^{\frac{x-5}{ 1+x }} + 5$	$x \neq -1$
136	$y = 6x^2 - ex - 3 \log_4(e^x - e^{\sqrt{3}})$	$x > \sqrt{3}$
137	$y = 3x - \frac{2 - \ln(x-1)}{4 + \ln^2 x}$	$x > 1$
138	$y = x-5 e^{\frac{5^x}{2-x}}$	$x \neq 2$
139	$y = x+6 \ln x^2 - 5 $	$x \neq -\sqrt{5} \wedge x \neq \sqrt{5}$
140	$y = \frac{\sqrt{3^{4x} + 7 \cdot 3^{2x} + 10}}{7^{\frac{3x-e}{x}}}$	$x \neq 0$
141	$y = x^\pi$	$x \geq 0$
142	$y = (\sqrt[3]{3})^{\ln x}$	$x > 0$
143	$y = \frac{3^{2x} + 3^x - 1}{\ln \frac{x+1}{x}}$	$x < -1 \vee x > 0$

144	$y = 2^{\frac{\sqrt{x^2-e^2}}{x+1}}$	$x < -e \vee x > e$
145	$y = 3x - e^{\frac{1}{1-\ln x}}$	$x > 0 \wedge x \neq e$
146	$y = e^{\frac{3}{\ln x - 2}}$	$x > 0 \wedge x \neq e^2$
147	$y = \log_{\frac{1}{2}} \frac{2-x}{9-x^2}$	$-3 < x < 2 \vee x > 3$
148	$y = \log_2 \frac{x+5}{1-x^2}$	$x < -5 \vee -1 < x < 1$
149	$y = 5^{\frac{x}{2-x^2}}$	$x \neq -\sqrt{2} \wedge x \neq \sqrt{2}$
150	$y = 2^{\frac{x+1}{x^2-4}}$	$x \neq -2 \wedge x \neq 2$
151	$y = e^{\frac{\sqrt{x^2-7x+12}}{x-5}}$	$x < 3 \vee 4 \leq x < 5 \vee x > 5$
152	$y = \left(\frac{3}{4}\right)^{\sqrt{2-x^2}}$	$-\sqrt{2} \leq x \leq \sqrt{2}$

153	$y = \sqrt{\left(\frac{1}{2}\right)^{\frac{x-3}{x+5}} - \frac{1}{8}}$	$x \leq -9 \vee x > -5$
154	$y = \frac{3^{\frac{1}{x+1}} - 5^x}{\left(\frac{1}{4}\right)^{x^2} - 1}$	$x \neq -1 \wedge x \neq 0$
155	$y = \log_7(e^{2x} - 5e^x + 6) + \log_7 x - 2 $	$x < \ln 2 \vee \ln 3 < x < 2 \vee x > 2$
156	$y = \frac{\log_2(x + 1) + 2^{\frac{x}{x-1}}}{2^{\sqrt{x}}}$	$0 \leq x < 1 \vee x > 1$
157	$y = 2 \cdot 3^x \ln(2x - \sqrt[3]{x}) - 3$	$x < -\frac{\sqrt{2}}{4} \vee x > \frac{\sqrt{2}}{4}$
158	$y = \frac{3^x + \ln x - 1}{\ln^2 x - 7 \ln x + 10}$	$x > 0 \wedge x \neq e^2 \wedge x \neq e^5$
159	$y = \ln \ln(x - 2)$	$x > 3$
160	$y = \ln \frac{x^2 - 9}{x - 2} + e^{\sqrt{x^4 - 16}}$	$-3 < x \leq -2 \vee x > 3$
161	$y = 3^{\frac{x}{5 - \sqrt{x - x^2}}}$	$0 \leq x \leq 1$
162	$y = \sqrt{9 \cdot 3^{2x} - 82 \cdot 3^x + 9}$	$x \leq -2 \vee x \geq 2$

163	$y = e^x \log_{\frac{1}{3}}(3-x) + \log_5(1-x^2) + \log_5 x$	$0 < x < 1$
164	$y = \sqrt{\frac{\ln(2^x - 1)}{3^x - 1}}$	$x > 1$
165	$y = \sqrt[4]{\log_{\frac{1}{2}}(x^2 - 4) - \log_{\frac{1}{2}}(x - 1)}$	$2 < x \leq \frac{1 + \sqrt{13}}{2}$
166	$y = \frac{x^2 + 2x - 3}{\ln^2(2x - 3) - 1}$	$x > \frac{3}{2} \wedge x \neq \frac{3+e}{2} \wedge x \neq \frac{1+3e}{2}$
167	$y = \frac{\ln x - 5}{\ln^2 x^2 - 1}$	$x > 0 \wedge x \neq \sqrt{e^{-1}} \wedge x \neq \sqrt{e}$
168	$y = \frac{1 - 3x^2}{\ln(5x^2 - 12)}$	$x < -\frac{2\sqrt{15}}{2} \vee x > \frac{2\sqrt{15}}{2} \wedge x \neq \pm \frac{\sqrt{65}}{5}$
169	$y = (e^{2x} - 5e^x + 6)^{x^2 - 3x}$	$x < \ln 2 \vee x > \ln 3$
170	$y = \frac{3 + \log_4(x^2 + 1)}{\log_x 5}$	$0 < x < 1 \vee x > 1$
171	$y = \sqrt{\log_{\frac{1}{3}}(x^2 - 3x - 1)}$	$\frac{3 - \sqrt{17}}{2} \leq x < \frac{3 - \sqrt{13}}{2} \vee$ $\frac{3 + \sqrt{13}}{2} < x \leq \frac{3 + \sqrt{17}}{2}$
172	$y = \sqrt{\ln x^2 - 9 }$	$x < -\sqrt{10} \vee -2\sqrt{2} \leq x \leq 2\sqrt{2} \vee$ $x > \sqrt{10}$

173	$y = \log_3 \log_{\frac{1}{4}}(5x - 3)$	$\frac{3}{5} < x < \frac{4}{5}$
174	$y = \ln \ln(x^2 - 3)$	$x < -2 \vee x > 2$
175	$y = \frac{\ln(2 - x - 3)}{\sqrt{\log_2 x - 2}}$	$4 < x < 5$
176	$y = \left(\frac{3x - 4}{4x - 1}\right)^{\frac{x-1}{x-3}}$	$x < \frac{1}{4} \vee \frac{4}{3} < x < 3 \vee x > 3$
177	$y = \frac{2^x + 5}{\sqrt{\log_3(x - 2x^2) + 2}}$	$\frac{1}{6} < x < \frac{1}{3}$
178	$y = \frac{\sqrt[3]{2x^2 - x + 5}}{\sqrt{\ln x }}$	$x < -1 \vee x > 1$
179	$y = \frac{e^{-x^2+3x}}{\ln(x^2 - 2 + 3x)}$	$x < -\frac{\sqrt{17}+3}{2} \vee x > \frac{3-\sqrt{17}}{2} \wedge$ $x \neq -\frac{\sqrt{21}+3}{2} \wedge x \neq \frac{3-\sqrt{13}}{2}$
180	$y = \frac{2^{2x} - 6}{\ln x^2 - 8 }$	$x \neq \pm 2\sqrt{2} \wedge x \neq \pm 3 \wedge x \neq \pm\sqrt{7}$
181	$y = \frac{\ln \sqrt{\frac{x(x-1)}{x+5}}}{\frac{3x}{e^{x+1}} - 2}$	$-5 < x < -1 \vee -1 < x < 0 \vee x > 1$
182	$y = \sqrt[3]{\frac{x(x+2)}{2^{2-x}} - 1}$ $\sqrt{\log_3(x - 1)}$	$x < -1 \vee x > 1 \wedge x \neq \pm 2$

183	$y = \left(\log_{\frac{2}{3}}(x-3)\right)^{\frac{x+2}{x}}$	$3 < x < 4$
funzioni goniometriche 		
187	$y = \sin x \cdot \cos x$	\mathbb{R}
188	$y = \sqrt[3]{6 + \cos x}$	\mathbb{R}
189	$y = \frac{2 + x^2 - 4x}{\sin x}$	$x \neq k\pi$
190	$y = \frac{2 - \cos^4 x}{\sin^2 x + 2}$	\mathbb{R}
191	$y = 4 \sin x - 3 \cos 3x$	\mathbb{R}
192	$y = \sin\left(x^2 - \frac{\pi}{6}\right)$	\mathbb{R}
193	$y = \sin \cos \ln x$	$x > 0$
194	$y = \frac{3}{\sin x}$	$x \neq k\pi$
195	$y = \arctan \left \frac{2-5x}{3-x} \right $	$x \neq 3$
196	$y = \ln(\sin x - 1)$	\emptyset
197	$y = \frac{1 + \tan x}{\sqrt{\cos^2 x - 1}}$	\emptyset
198	$y = \frac{\arcsin x - \pi}{x^2 - 1}$	$-1 < x < 1$

199	$y = \operatorname{arccot} \sqrt{x^2 - 9}$	$x \leq -3 \vee x \geq 3$
200	$y = \frac{\sin 3x + 2}{\cos 2x - 1}$	$x \neq k\pi$
201	$y = \sqrt{\arcsin(x - 2)}$	$2 \leq x \leq 3$
202	$y = \frac{2 \cos x - 1}{\sin x + 1}$	$x \neq \frac{3}{2}\pi + 2k\pi$
203	$y = \frac{\arctan x + \sin x}{2 + x}$	$x \neq -2$
204	$y = \log_{10} \tan x$	$\frac{\pi}{4} + k\pi < x < \frac{\pi}{2} + k\pi$
205	$y = \sqrt{-\cos 2x}$	$\frac{\pi}{4} + k\pi \leq x \leq \frac{3}{4}\pi + k\pi$
206	$y = \log_2(-\sin 3x)$	$\frac{\pi}{3} + \frac{2}{3}k\pi < x < \frac{2}{3}\pi + \frac{2}{3}k\pi$
207	$y = \ln \sin\left(x - \frac{\pi}{2}\right)$	$\frac{\pi}{2} + 2k\pi < x < \frac{3}{2}\pi + 2k\pi$
208	$y = \sqrt{x} + \arccos x$	$0 \leq x \leq 1$
209	$y = \ln \arctan x$	$x > 0$
210	$y = \sqrt[6]{\cos x}$	$-\frac{\pi}{2} + 2k\pi < x < \frac{\pi}{2} + 2k\pi$
211	$y = \frac{\cos x}{ 1 - \cos x }$	$x \neq 2k\pi$
212	$y = \frac{(x - 1) \cos x}{\cos^6 x + \sin^2 x}$	R

213	$y = 3 \frac{1}{\cos x}$	$x \neq \frac{\pi}{2} + k\pi$
214	$y = \arcsin \cos x$	\mathbb{R}
215	$y = (x - 1) \arctan \frac{x - 1}{x + 3}$	$x \neq -3$
216	$y = 5x + \arctan \frac{2x - 3}{3x + 5}$	$x \neq -\frac{5}{3}$
217	$y = \arctan(\ln(x + 1)^2)$	$x \neq -1$
218	$y = \sec 3x$	$x \neq \frac{\pi}{6} + k\frac{\pi}{3}$
219	$y = \sin\left(\frac{3}{2}x\right) + \ln \cos(2x)$	$-\frac{\pi}{4} + k\pi < x < \frac{\pi}{4} + k\pi$
220	$y = \log_7(\cot x - \sqrt{3})$	$k\pi < x < \frac{\pi}{6} + k\pi$
221	$y = 2\sqrt{\left \frac{\sin x}{1 - 2\cos x}\right }$	$x \neq \pm \frac{\pi}{3} + 2k\pi$
222	$y = \sqrt{\frac{1 - \cos x}{1 - \sin x}}$	$x \neq \frac{\pi}{2} + 2k\pi$

223	$y = \arccos \frac{x+1}{x-2}$	$x \leq \frac{1}{2}$
224	$y = \frac{5 - 2\cos \frac{x}{2}}{\sin \left(\frac{x}{2}\right) + \frac{\sqrt{3}}{2}}$	$x \neq -\frac{2}{3}\pi + 4k\pi \wedge x \neq \frac{8}{3}\pi + 4k\pi$
225	$y = 2 - \frac{\cos x - \sqrt{3}}{\tan x + 1}$	$x \neq -\frac{\pi}{4} + k\pi \wedge x \neq \frac{\pi}{2} + k\pi$
226	$y = \tan \frac{x}{3} - \frac{2+x}{2 \cot x}$	$x \neq \frac{3\pi}{2} + 3k\pi \wedge x \neq \frac{\pi}{2} + k\pi$
227	$y = \frac{\tan x \cos x}{1 - \sin x \cot x}$	$x \neq 2k\pi$
228	$y = \frac{2}{\sqrt{\cos \frac{x}{2} - \frac{1}{2}}}$	$-\frac{2\pi}{3} + 4k\pi < x < \frac{2\pi}{3} + 4k\pi$
229	$y = \ln \left(1 - 2\cos \frac{x}{2}\right)$	$\frac{2}{3}\pi + 4k\pi < x \leq \frac{10}{3}\pi + 4k\pi$
230	$y = \arcsin(1 - \sqrt{x+3})$	$-3 \leq x \leq 1$
231	$y = \frac{2\cos x + 3\sin x}{5\arctan(2\ln x)}$	$x > 0 \wedge x \neq 1$
232	$y = \csc x + \arcsin x$	$-1 \leq x \leq 1 \wedge x \neq 0$

233	$y = \tan(x - 3) + \sqrt{\ln(x^2 + 1)}$	$x \neq \frac{\pi}{2} + 3 + k\pi$
234	$y = \arcsin(9 - x^2)$	$-\sqrt{10} \leq x \leq -2\sqrt{2} \vee 2\sqrt{2} \leq x \leq \sqrt{10}$
235	$y = \arcsin \frac{3 \ln x + 1}{\ln x - 1}$	$\frac{1}{e} \leq x \leq 1$
236	$y = \log_2 \arccos \ln x$	$\frac{1}{e} \leq x < e$
237	$y = \arcsin \ln x - \ln \arcsin x$	$\frac{1}{e} \leq x \leq 1$
238	$y = \sqrt{\sin x + \cos x}$	$-\frac{\pi}{4} + 2k\pi \leq x \leq \frac{3}{4}\pi + 2k\pi$
239	$y = \sqrt{\frac{2 \sin x - 1}{\cot x}}$	$\frac{\pi}{6} + 2k\pi \leq x < \frac{\pi}{2} + 2k\pi \vee$ $\frac{5}{6}\pi + 2k\pi \leq x < (2k + 1)\pi \vee$ $+2k\pi < x < 2(k + 1)\pi$
240	$y = \arcsin \frac{3}{x^2 - 4}$	$x \leq -\sqrt{7} \vee -1 \leq x \leq 1 \vee x \geq \sqrt{7}$
241	$y = \frac{3 \sin x + \cos x}{\sqrt[4]{ \tan x - \sqrt{3} }}$	$x \neq \frac{\pi}{3} + k\pi \wedge x \neq \frac{\pi}{2} + k\pi$
242	$y = \arccos \frac{1}{\tan x}$	$\frac{\pi}{4} + k\pi \leq x \leq \frac{3}{4}\pi + k\pi$
243	$y = \sqrt{\frac{\cos x}{1 - \cos 2x}}$	$2k\pi < x \leq \frac{\pi}{2} + 2k\pi \vee$ $\frac{3}{2}\pi + 2k\pi \leq x < 2\pi + 2k\pi$

244	$y = \log_3 \arcsin(e^x - 2)$	$\ln 2 < x \leq \ln 3$
245	$y = \frac{\cos x}{\ln \cos x }$	$x \neq \frac{\pi}{2}k$
246	$y = \log_3(\tan x + 3 \cot x - 4)$	$k\pi < x < \frac{\pi}{4} + k\pi \vee$ $\arctg 3 < x < \frac{\pi}{2} + k\pi$
247	$y = \operatorname{arccot}(3x - 2\sqrt[4]{5 - 7x})$	$x \leq \frac{5}{7}$
248	$y = \frac{1 - 2 \sin^2 x}{1 - 2 \cos x}$	$x \neq \frac{\pi}{3} + 2k\pi \wedge x \neq \frac{5}{3}\pi + 2k\pi$
249	$y = \arcsin \sqrt{x - 2x^2}$	$0 \leq x \leq \frac{1}{2}$
250	$y = \sqrt{\sqrt{3} \sin^2 x - \sin x \cos x}$	$\frac{\pi}{6} + k\pi \leq x \leq (k + 1)\pi$
251	$y = \frac{3 - \tan x}{\sin 2x - \cos x}$	$x \neq \frac{5\pi}{6} + 2k\pi \wedge x \neq \frac{\pi}{6} + 2k\pi \wedge$ $x \neq \frac{\pi}{2} + k\pi$
252	$y = \cot \frac{x}{2} \left(1 - \frac{\tan^2 x}{\sqrt{1 - \tan x}} \right)$	$-\frac{\pi}{2} + k\pi < x < \frac{\pi}{4} + k\pi \wedge x \neq k\pi$
253	$y = \sqrt[4]{\frac{\sin x \cos x - 1}{\sqrt{3} - \cot x}}$	$k\pi < x < \frac{\pi}{6} + k\pi$

esercizi di riepilogo



254	$y = x^{2^x+3}$	$x > 0$
255	$y = \sqrt[3]{2xe^x - 2x}$	\mathbb{R}
256	$y = 1 - e^{\frac{\sin x}{\cos^2 x - 1}}$	$x \neq k\pi$
257	$y = \sqrt{\arcsin \frac{2x^2}{x+1}}$	$-\frac{1}{2} \leq x \leq 1$
258	$y = \ln \arctan x$	$x > 0$
259	$y = \ln \left(\frac{4^x - 2^x}{5^x + 3} \right)$	$x > 0$
260	$y = \left(\frac{1}{5} \right)^{\arccos \ln x}$	$\frac{1}{e} \leq x \leq e$
261	$y = \ln(x)^{\frac{\ln x}{x}}$	$x > 1$
262	$y = \arctan \arccos \sin \frac{1}{x}$	$x \neq 0$
263	$y = \sin \ln \cos x$	$-\frac{\pi}{2} + 2k\pi < x < \frac{\pi}{2} + 2k\pi$

264	$y = \frac{\sqrt[4]{x^2 - 4}}{\sqrt{4 - 3x}}$	$x \leq -2 \vee \frac{4}{3} < x \leq 2$
265	$y = \frac{\sqrt{1 - 2x^2}}{\arccos(7x - 1)}$	$0 \leq x < \frac{2}{7}$
266	$y = \frac{\arctan(\sqrt{x} - 5)}{\ln 5 - x^2 }$	$0 \leq x < \sqrt{6} \vee x > \sqrt{6} \wedge$ $x \neq 2 \wedge x \neq \sqrt{5}$
267	$y = \left(\frac{x + 1}{x^2}\right)^{\sin x}$	$x > -1 \wedge x \neq 0$
268	$y = \frac{\sqrt{\log_2(x - 1)}}{\sin x (\cos x - 1)}$	$x \geq 2 \wedge x \neq k\pi$
269	$y = \frac{\sqrt{e^{\frac{1}{2}\tan x}}}{\log_3(x^2 - x) - 2}$	$x < 0 \vee x > 1 \wedge x \neq \frac{\pi}{2} + k\pi \wedge$ $x \neq \frac{1 \pm \sqrt{37}}{2}$
270	$y = \frac{\ln \sin x}{\ln \cos x}$	$2k\pi < x < \frac{\pi}{2} + 2k\pi$
271	$y = \sqrt{1 + \frac{\pi}{\arcsin x}}$	$0 < x \leq 1$
272	$y = \frac{\sqrt[3]{3 - \arcsin x}}{\sqrt[4]{\arctan \frac{x}{2} + \pi}}$	$-1 \leq x \leq 1$
273	$y = \frac{x - 1}{\pi - \arctan x }$	R

274	$y = \arctan \sqrt{\frac{x^2 - 4}{x - 1}}$	$-2 \leq x < 1 \vee x \geq 2$
275	$y = \frac{x(x - 3)}{2 \arccos x - \pi}$	$-1 \leq x < 0 \vee 0 < x \leq 1$
276	$y = \sqrt[3]{\frac{x^2 - 1}{ 4 - x^2 }}$	$x \neq -2 \wedge x \neq 2$
277	$y = \sqrt{\frac{x^2 - 1}{2x + 1}} + \sqrt{\frac{3x}{2 - x^2}}$	$1 \leq x < \sqrt{2}$
278	$y = \left[\log_{\frac{1}{3}}(x^2 - 3) \right]^e$	$-2 \leq x < -\sqrt{3} \vee \sqrt{3} \leq x < 2$
279	$y = \sqrt{2 - e^x - 3 }$	$0 \leq x \leq \ln 5$
280	$y = \frac{1}{\arccos(2x)} - \frac{1}{\arcsin(3x)}$	$-\frac{1}{3} \leq x \leq \frac{1}{3} \wedge x \neq 0$
281	$y = \ln \frac{x^2 - 9}{x - 2} + e^{\sqrt{x^4 - 16}}$	$-3 < x \leq -2 \vee x > 3$
282	$y = \sqrt{\frac{2 \cos^2 x + 3 \sin x - 3}{1 - 2 \sin^2 x - \cos x}} \quad \text{con } x \in [0, 2\pi]$	$0 < x \leq \frac{\pi}{6} \vee \frac{2}{3}\pi < x \leq \frac{5}{6}\pi \vee \frac{4}{3}\pi < x < 2\pi$
283	$y = (\sin x - \cos x)^{\ln \sqrt{2 \sin x - 1}} \quad \text{con } x \in [0, 2\pi]$	$\frac{\pi}{4} \leq x < \frac{5}{6}\pi$

284	$y = \sqrt{x + 1 - \sqrt[3]{x^3 + 2x^2 + 3x + 6}}$	$x \leq -\sqrt{5} \vee x \geq \sqrt{5}$
285	$y = \frac{5}{x-1} \ln \frac{e^x - 1}{x-1}$	$x < 0 \vee x > 1$
286	$y = \arccos[\ln(1-x) - \ln(x+1)]$	$\frac{1-e}{1+e} \leq x \leq \frac{e-1}{e+1}$
287	$y = \arcsin \frac{\tan^2 x}{3}$	$-\frac{\pi}{3} + k\pi \leq x \leq \frac{\pi}{3} + k\pi$
288	$y = \sqrt{\arcsin \ln(x+2)}$	$-1 \leq x \leq e-2$
289	$y = \sqrt{\frac{x^3 - 1}{x^2 - 9x + 18}} + e^{\frac{1}{\tan x}}$	$1 \leq x < 3 \vee x > 6 \wedge x \neq k\frac{\pi}{2}$
290	$y = \frac{\tan \ln 2x}{\ln \tan 2x}$	$k\frac{\pi}{2} < x < \frac{\pi}{8} + k\frac{\pi}{2} \vee$ $\frac{\pi}{8} + k\frac{\pi}{2} < x < \frac{\pi}{4} + k\frac{\pi}{2} \wedge$ $x \neq \frac{1}{2}e^{\frac{\pi}{2} + k\pi} \quad k \in \mathbb{N}$
291	$y = \sqrt{\log_{\frac{1}{2}} \arccos x + \log_2 \frac{\pi}{3}}$	$\frac{1}{2} \leq x < 1$
292	$y = \frac{\sqrt{\arcsin x - \frac{\pi}{3}}}{\ln x}$	$\frac{\sqrt{3}}{2} \leq x < 1$
293	$y = \frac{1}{2 \ln 3x - 1} + \ln \arcsin x$	$0 < x < \frac{\sqrt{e}}{3} \vee \frac{\sqrt{e}}{3} < x \leq 1$

294	$y = 1 - e^{ \sin x - 1} + e^{\frac{1}{\sqrt{1 - \tan x}}}$	$-\frac{\pi}{2} + k\pi < x < \frac{\pi}{4} + k\pi$
295	$y = \ln(x^2 - x - 4) + \arccos \ln x$	$\frac{1 + \sqrt{17}}{2} < x \leq e$
296	$y = \arcsin \frac{\ln x - 1}{\ln x - 2}$	$0 < x \leq e\sqrt{e}$
297	$y = \sqrt{\log_3^2 x - \log_3 x - 2 }$	$0 < x \leq \frac{1}{9} \vee x \geq 3$
298	$y = \frac{x^2 + 1 + \sqrt{8 - x^3}}{\sqrt{3 - x} - x + 3}$	$x \leq 2$
299	$y = \log_3(3 - x - 3 - x - 2)$	$x > 1$
300	$y = [\log_2(x^2 - 4x + 4)]^{\sqrt{2}}$	$x \leq 1 \vee x \geq 3$
301	$y = \ln(2\sin^2 x - \sin x - 1) \quad \text{con } x \in [0, 2\pi]$	$\frac{7}{6}\pi < x < \frac{11}{6}\pi$
302	$y = \arccos(x^2 - 10x + 1)$	$0 \leq x \leq 5 - \sqrt{23} \vee 5 + \sqrt{23} \leq x \leq 10$
303	$y = \arcsin \tan x + \frac{1}{\arccos \sin x}$	$-\frac{\pi}{4} + k\pi \leq x \leq \frac{\pi}{4} + k\pi$
304	$y = \sqrt{\frac{\arcsin 2x}{\arctan x - \frac{\pi}{3}}}$	$-\frac{1}{2} \leq x \leq 0$

305 $y = \ln(|x^2 - x| - 4) + \arccos \ln x$

$$\frac{1 + \sqrt{17}}{2} < x \leq e$$

esercizi di riepilogo più impegnativi



306 $y = \sqrt{3x - |x - |2x^2 - 1||}$

$$\frac{\sqrt{6} - 2}{2} \leq x \leq \frac{\sqrt{6} + 2}{2}$$

307 $y = \sqrt{\log_{x-1} \frac{3x^2 + 10x + 3}{11}}$

$$x > 2$$

308 $y = \sqrt{\log_2(|x + 3| - 3) - \log_2(|x + 7| + 1)}$

$$x \leq -7$$

309 $y = \arccos(-3 + \sqrt{24 \sin^2 x - 2})$

$$\frac{\pi}{6} + k\pi \leq x \leq \frac{\pi}{3} + k\pi \vee$$
$$-\frac{\pi}{3} + k\pi \leq x \leq -\frac{\pi}{6} + k\pi$$

310 $y = \frac{\ln(\sqrt{9x^2 - 30x + 25} - \sqrt{x^2 + 5x - 6})}{x - 3 - \sqrt{x^2 - 4}}$

$$x \leq 6 \vee 1 \leq x < \frac{35 - \sqrt{233}}{16} \vee$$
$$x > \frac{35 + \sqrt{233}}{16}$$

311 $y = \frac{\sqrt{\frac{\pi}{4} - \arctan \sin x}}{|\cot 2x| - \sqrt{3}}$

$$x \neq \pm \frac{\pi}{12} + k\frac{\pi}{2} \wedge x \neq k\frac{\pi}{2}$$

312 $y = e^{\sqrt{\frac{\sin^2 x - \frac{1}{2}}{\cos^3 x}}}$

$$\frac{\pi}{4} + 2k\pi \leq x < \frac{\pi}{2} + 2k\pi \vee$$
$$\frac{3\pi}{4} + 2k\pi \leq x \leq \frac{5\pi}{4} + 2k\pi \vee$$
$$\frac{3\pi}{2} + 2k\pi < x \leq \frac{7\pi}{4} + 2k\pi$$

313 $y = \sqrt{\frac{\ln \arctan(x^2 - x) - \ln \frac{\pi}{4}}{e^{\frac{1}{2x}} - 1}}$

$$\frac{1 - \sqrt{5}}{2} \leq x < 0 \vee x \geq \frac{1 + \sqrt{5}}{2}$$

314	$y = \sqrt{\log_{\frac{1}{2}} \arccos x + \log_2 \frac{\pi}{3}}$	$\frac{1}{2} \leq x < 1$
315	$y = \frac{1}{\sqrt[4]{x^2 - 5x + 6} - \sqrt{x - 1}}$	$1 \leq x < \frac{5}{3} \vee \frac{5}{3} < x \leq 2 \vee x \geq 3$
316	$y = \frac{\sqrt{x^2 - 2x + 1} - 3}{\sqrt{ x } - \sqrt{x + 1}}$	$-1 \leq x < -\frac{1}{2} \vee x > -\frac{1}{2}$
317	$y = \frac{ x - 1 + \sqrt{x}}{\sqrt{3 - x^2 - 5x + 6 } - \sqrt{x + 1}}$	$\frac{5 - \sqrt{13}}{2} \leq x \leq \frac{5 + \sqrt{13}}{2} \wedge x \neq 2$
318	$y = \frac{\sqrt{x + x^2 - 1 } - 3}{\sqrt{x + \sqrt{x - 1}}}$	$x \geq 1$
319	$y = \sqrt{\frac{x^2 - x + 3 }{\sqrt{x - 1} + x + 3 }}$	$x \geq \frac{1 + \sqrt{13}}{2}$
320	$y = \sqrt{x - \sqrt{2x + 3}} + \sqrt{x^3 - 3x^2}$	$x \geq 3$
321	$y = \sqrt[4]{x^5 + x^3} + \sqrt{\sqrt{3x - 2} - 5}$	$x \geq 9$

322	$y = \sqrt{\frac{\log_1(x-3) + 2}{3 + \log_{x+1} 5}}$	$3 < x \leq 7$
323	$y = \log_{x-5}(x-2)$	$5 < x < 6 \vee x > 6$
324	$y = \ln \ln x $	$x \neq -1 \wedge x \neq 0 \wedge x \neq 1$
325	$y = \ln \left(2 - \left \frac{x}{1-3x} \right \right)$	$x < \frac{2}{7} \vee x > \frac{2}{5}$
326	$y = \sqrt{\frac{\log_x x-5 }{e^{\ln \frac{2x(x-4)}{x+1}}}}$	$x \geq 6$
327	$y = \frac{3 + e^{-\frac{x^2-3x+2}{x-6}}}{\log_{\frac{3}{4}} \sqrt{x^2 - \frac{1}{4}}}$	$x < -\frac{1}{2} \vee x > \frac{1}{2} \wedge$ $x \neq \pm \frac{\sqrt{5}}{2} \wedge x \neq 6$
328	$y = \frac{\sqrt{\sin x \left(\cos x - \frac{1}{2} \right)}}{ \tan x - 1}$	$2k \leq x \leq \frac{\pi}{3} + 2k\pi \vee$ $\pi + 2k\pi \leq x \leq \frac{5\pi}{3} + 2k\pi \wedge$ $x \neq \frac{3}{2}\pi + 2k\pi \wedge x \neq \frac{\pi}{4} + k\pi$
329	$y = \frac{\sqrt{ \cos x - \frac{1}{2}}}{e^{\frac{1}{\sin x}}}$	$-\frac{\pi}{3} + k\pi \leq x \leq \frac{\pi}{3} + k\pi \wedge x \neq k\pi$

330	$y = \frac{\ln(\sin x - 1)}{\ln \sqrt{\cos x}}$	\emptyset
331	$y = e^{\frac{\tan x}{ \cos x - \frac{\sqrt{2}}{2}}}$	$x \neq \frac{\pi}{2} + k\pi \wedge x \neq \frac{\pi}{4} + k\frac{\pi}{2}$
332	$y = \frac{\sqrt{\arcsin(2 x - 1)}}{\ln(2x^3 - x)}$	$-\frac{\sqrt{2}}{2} \leq x \leq -\frac{1}{2} \vee \frac{\sqrt{2}}{2} < x < 1$
333	$y = \frac{\ln \ln(x - 1 - 5)}{1 - e^{\frac{x}{\sqrt{x - 1 - x }}}}$	$x > 7$
334	$y = \frac{1}{3} \frac{\ln \ln \frac{1}{\sqrt{x^2 + 3x - 10}}}{\sqrt{ x - 1 - x^2}}$	\emptyset
335	$y = \frac{\sqrt{x} \sqrt{e^{x+1} + 3}}{\sqrt{x^2 - 4x + 4}}$	$x > 0 \wedge x \neq 2 \wedge x \in \mathbb{N}$
336	$y = \frac{\left \ln \frac{x^2 + x - 1}{x - 2} - 1 \right }{\sqrt{x}}$	$0 < x < \frac{1}{2}(\sqrt{5} - 1) \vee x > 2$
337	$y = e^x \ln \left(2^{\frac{x^2 - 1}{2x}} + x e^x \right)$	$x > 0$
338	$y = \ln \left(\sin x - \frac{\sqrt{3}}{2} \right) + \ln \sqrt{\cos x} - \ln \left(\tan \frac{x}{2} + 1 \right)$	$\frac{\pi}{3} + 2k\pi < x < \frac{\pi}{2} + 2k\pi$

339	$y = \log_{\frac{1}{2}} \frac{x^2 - 1}{x^2 + 1} + 3^{\frac{x}{\sqrt{x-1}}} \log_2 \frac{1}{x+2} - \sqrt{2} e^{\frac{1}{\ln x}} \log_2 \sqrt{\frac{x}{x+1}}$	$x > 1$
340	$y = \sqrt{\log_a(x^2 + 2x + 4) - \log_a(x^2 + x + 3)} + \log_a(a^{x^2+3x} - a^4)$ <p style="text-align: center;"><i>con $a \in \mathbb{R}^+ - \{1\}$</i></p>	<p style="text-align: right;"><i>se $a > 1 \rightarrow x > 1$</i></p> <p style="text-align: right;"><i>se $0 < a < 1 \rightarrow -4 \leq x \leq -1$</i></p>

